Title:DARK MATTER:FLAT ROTATION CURVE OF GALAXIES-TULLY-FISHER

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#### Abstract:

The article proposes a new model of dark matter. According to this new model, dark matter is a substance, that is a new physical element not constituted of classical particles, called *dark substance*, filling the universe and constituting what is called "emptiness". Assuming some very simple physical properties to this dark substance, we theoretically justify the flat rotation curve of galaxies and the baryonic Tully-Fisher's law. We will then see how the new model of dark matter can be generalized to scales larger than galactic (galaxy clusters) and also to structure formation. Finally we will see how the new model of dark matter permits to interpret dark energy and the Cosmological parameters relative to the expansion of the Universe (ΛCDM model).

Key words: Tully-Fisher's law, dark matter, dark halo, flat rotation curve of galaxies, dark radius, dark energy, ΛCDM model, structure formation, galaxy clusters.

### 1.INTRODUCTION

The objective of this study is to propose fundamental theoretical discoveries relative to nature of dark matter. In this article, we propose that a new physical element, called dark substance, constitutes the dark matter. This dark substance constitutes also what is called emptiness. According to the proposed model of dark matter, this dark substance fills all the Universe and has physical properties close to the physical properties of an ideal gas. Using those properties, we justify theoretically the flat rotation curve that is observed for some galaxies, in a new way, with density of dark substance in  $1/r^2$ . A simple mathematical expression of the density of dark matter (in  $1/r^2$ ) permitting to obtain the flat rotation curve which has already been proposed, but the model of dark matter that permits to justify theoretically this mathematical expression (in  $1/r^2$ ) has never been proposed. Moreover the study hypothesizes simple thermal properties to this dark substance which exist in our model of dark matter that permit to justify theoretically the baryonic Tully-Fisher's law. The theory called MOND [1] also proposes a theoretical justification of the flat rotation curve of some galaxies, but this theory is contrary to Newton's attraction law and moreover it is contradicted by some astronomical observations [2]. Different models of distribution of dark matter in galaxies are proposed in this study.

We remind that for many astrophysicists and physicists, the enigmas in the SCM, in particular the enigmas concerning dark matter and dark energy, make necessary a new paradigm for the SCM [3]. Our article proposes a new model of dark matter that could belong to such a new paradigm.

The model of dark matter that we propose is compatible with the Standard Cosmological Model (SCM) as it is presented in books [4][5][6].

Indeed, we will show that the new model of dark matter can be generalized to scales larger than galactic (galaxy clusters), to structure formation and to interpret dark energy and the Cosmological parameters relative to the expansion of the Universe ( $\Lambda$ CDM model).

#### 2. THEORY OF DARK MATTER

## 2.1 Physical properties of the dark substance.

As we have seen in 1.INTRODUCTION, we stated the Postulate 1 expressing the physical properties of the dark substance:

#### Postulate 1:

a)A substance, called *dark substance*, fills all the Universe, constituting what is called *emptiness*.

b)This substance behaves as absolute emptiness with photons crossing it and consequently does not interact with them.

c)This substance owns a mass and obeys to the Boyle's law, to the Charles'law and also to the following law that is their synthesis:

An element of dark substance with a mass m, a volume V, a pressure P and a temperature T verifies,  $k_0$  being a constant:

 $PV=k_0mT$ 

The preceding law is a valid statement for a given ideal gas  $G_0$ , replacing  $k_0$  by a constant  $k(G_0)$ , and this is a consequence of the *universal gas equation*, which is also obtained using Boyle and Charles'laws.

We have 2 remarks consequences of this Postulate1:

-First, the dark substance is not really dark but translucent despite of its name. Indeed, because of the preceding Postulate 1b) it does not interact with photons crossing it.

-Secondly because of the Postulate 1a), what is usually called "emptiness" is not empty in reality: It is filled with dark substance.

### 2.2 Flat rotation curves of galaxies.

Using the fact that the dark substance behaves as an ideal gas (Postulate 1c), we are going to show that a spherical concentration of dark substance in gravitational equilibrium can constitute the dark matter in a galaxy with a flat rotation curve.

According to Postulate 1c) an element of dark substance with a mass m, a volume V, a pressure P and a temperature T verifies the law,  $k_0$  being a constant:

$$PV=k_0mT$$
 (1)

Which means, setting  $k_1=k_0T$ :

$$PV=k_1m$$
 (2)

Or equivalently,  $\rho$  being the mass density of the element:

$$P=k_1\rho$$
 (3a)

We hypothesized that the galaxy can be modeled as a concentration of dark substance with a spherical symmetry, at an homogeneous temperature T, in gravitational equilibrium.

We considered the spherical surface S(r) (resp. the spherical surface S(r+dr)) that is the spherical surface with a radius r (resp. r+dr) and whose the centre is the center O of the galaxy. S(O,r) is the sphere filled with dark substance with a radius r and the centre O.

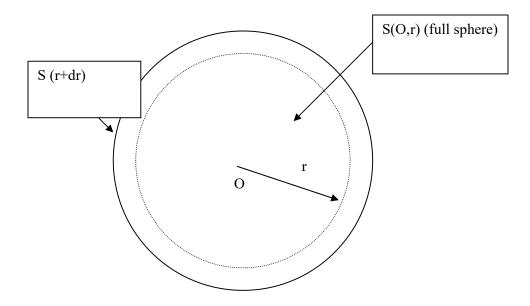


Figure 1:The spherical concentration of dark substance

The mass M(r) of the sphere S(O,r) is given by:

$$M(r) = \int_0^r \rho(x) 4\pi x^2 dx \tag{3b}$$

Assuming a spherical symmetry for the density of dark substance, using Newton's law  $(\Sigma \mathbf{F} = \mathbf{0})$  for a material element in equilibrium with a mass m,  $\mathbf{F}_G(\mathbf{r}) = \mathbf{m}\mathbf{G}(\mathbf{r})$ ,  $\mathbf{F}_G(\mathbf{r})$  gravitational force acting on the element,  $\mathbf{G}(\mathbf{r})$  gravitational field defined by Newton's universal law of gravitation) and Gauss theorem in order to obtain  $\mathbf{G}(\mathbf{r})$ , we obtain the following equation (4) of equilibrium of forces on an element dark substance with a surface dS, a width dr, situated between  $\mathbf{S}(\mathbf{O},\mathbf{r})$  and  $\mathbf{S}(\mathbf{r}+\mathbf{d}\mathbf{r})$ :

$$dSP(r+dr) + \frac{G}{r^2}(\rho(r)dSdr)(\int_0^r \rho(x)4\pi x^2 dx) - dSP(r) = 0$$
 (4)

Eliminating dS, we obtain the equation:

$$\frac{dP}{dr} = -\frac{G}{r^2}(\rho(r))(\int_0^r \rho(x)4\pi x^2 dx)$$
 (5)

And using the equation (3) obtained using the Boyle-Charles'law assumed in the Postulate 1, we obtain the equation:

$$k_1 \frac{d\rho}{dr} = -\frac{G}{r^2} (\rho(r)) \left( \int_0^r \rho(x) 4\pi x^2 dx \right)$$
 (6)

We then verify that the density of the dark substance  $\rho(r)$  satisfying the preceding equation of equilibrium is the evident solution:

$$\rho(r) = \frac{k_2}{4\pi r^2} \tag{7}$$

(A density of dark matter expressed as in Equation (7) has already been proposed to explain the flat rotation curve of spiral galaxies, but it has not been proposed a model of dark matter permitting to justify theoretically this density in  $1/r^2$  or to obtain the constant  $k_2$ . Here we give a theoretical justification of this density in  $1/r^2$  and we are going to give the expression of the constant  $k_2$  (Equation (8)). This is the consequence of the model of dark substance as an ideal gas, Postulate 1).

In order to obtain  $k_2$ , we replace  $\rho(r)$  given by the expression (7) inside the equation (6), and we obtain immediately that this equation is verified for the following expression of  $k_2$ :

$$k_2 = \frac{2k_1}{G} = \frac{2k_0T}{G} \tag{8}$$

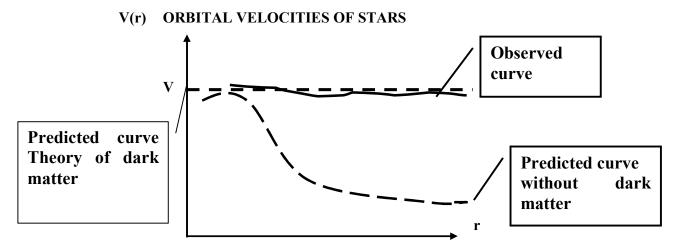
Using the preceding equation (7), we obtain that the mass M(r) of the sphere S(O,r) is given by the expression:

$$M(r) = \int_{0}^{r} 4\pi x^{2} \rho(x) dx = k_{2}r \quad (9)$$

We then obtain, neglecting the mass of stars in the galaxy, that the velocity v(r) of a star of a galaxy situated at a distance r from the center O of the galaxy is given by  $v(r)^2/r=GM(r)/r^2$  and consequently:

$$v(r)^2 = Gk_2 = 2k_1 = 2k_0T$$
 (10)

So we obtain in the previous equality (10) that the velocity of a star in a galaxy is independent of its distance to the centre O of the galaxy.



### DISTANCE OF STARS TO THE CENTRE O OF THE GALAXY

Figure 2: Rotation curve of galaxies

# 2.3 Baryonic Tully-Fisher's law.

### 2.3.1 Recall.

Tully and Fisher realized some observations on spiral galaxies with a flat rotation curve. They obtained that the luminosity L of such a spiral galaxy is proportional to the  $4^{th}$  power of the velocity v of stars in this galaxy [7]. So we have the Tully-Fisher's law for spiral galaxies,  $K_1$  being a constant:

$$L=K_1v^4$$
 (11)

But in the cases studied by Tully and Fisher, the baryonic mass M of a spiral galaxy is usually proportional to its luminosity L. So we have also the law for such a spiral galaxy, K<sub>2</sub> being a constant:

$$M = K_2 v^4$$
 (12)

This 2<sup>nd</sup> form of Tully-Fisher's law is known as the *baryonic Tully-Fisher's law*.

The more recent observations of Mc Gaugh [8] show that the baryonic Tully-Fisher's law (equation (12)) seems to be true for all galaxies with a flat rotation curve, including the galaxies with a luminosity not proportional to their baryonic mass.

We are going to demonstrate that using the Postulate 1 and a Postulate 2 expressing very simple thermal properties of the dark substance, (in particular its thermal interaction with baryonic particles), we can justify this baryonic law of Tully-Fisher.

## 2.3.2 Theory of quantified loss of calorific energy (by nuclei).

We saw in the previous equation (10) that according to our model of dark substance the square of the velocity of stars in a galaxy with a flat rotation curve is proportional to the temperature of the concentration of dark substance constituting this galaxy. So we need to determinate T:

-A first possible idea is that the temperature T refers on CMB. But this is impossible because it would imply all the stars of all galaxies with a flat rotation curve be driven with the same velocity and we know that it is not the case.

-The second possibility is that in the considered galaxy, each baryon interacts with the dark substance constituting the galaxy, transmitting to a thermal energy. We can expect that this thermal energy is very low otherwise it would already have been observed, but because of the expected very low density of the dark substance and of the considered times (we remind that the baryonic diameter of galaxies can reach 100000 light-years), it can lead to appreciable temperatures of dark substance. A priori we could expect that this loss of thermal energy for each baryon (transmitted to the dark substance) depends on the temperature of this baryon and of the temperature T of the dark substance in which the baryon is immerged, but if it was the case, the total lost thermal energy by all the baryons would be extremely difficult to calculate and moreover it should be very probable that we would then be unable to obtain the very simple baryonic Tully-Fisher's law.

The hypothesis of the study is defining the thermal transfer between dark substance and baryons, expressed in the following Postulate 2a) (Postulate 2 gives the thermal properties of the dark substance):

## Postulate 2a):

- -Each nucleus of atom in a galaxy is submitted to a loss of thermal energy, transmitted to the dark substance in which it is immerged.
- -This thermal transfer depends only on the number n of nucleons constituting the nucleus (So it is independent of the temperature of the nucleus). So if p is the thermal power dissipated by the nucleus, it exists a constant  $p_0$  (thermal power dissipated by nucleon) such that:

$$p=np_0 \tag{13}$$

According to the equation (13), the total thermal power transmitted by all the atoms of a galaxy towards the spherical concentration of dark matter constituting the galaxy is proportional to the total number of nucleons of the galaxy and consequently to the baryonic mass of this galaxy. So if  $m_0$  is the mass of one nucleon, M being the baryonic mass of the galaxy, we obtained according to the equation (13) that the total thermal power  $P_r$  received by the spherical concentration of dark substance constituting the galaxy from all the atoms is given by the following equation,  $K_3$  being the constant  $p_0/m_0$ :

$$P_r = (M/m_0)p_0 = K_3M$$
 (14)

Concerning the preceding Postulate 2a):

- -It is possible (but not compulsory) that it be true only for atoms whose temperature is superior to the temperature T of the concentration of dark substance.
- -It permits to obtain the very simple Equation (14). We will see that this equation is essential to obtain the baryonic Tully-Fisher's law.

#### 2.3.3 Obtainment of the baryonic Tully-Fisher's law.

In agreement with the previous model of galaxy (Section 2.2), we modeled a galaxy with a flat rotation curve as a spherical concentration of dark substance, at a temperature T and surrounded itself by a medium constituted of dark substance (called "intergalactic dark substance") with a temperature  $T_0$  and a density  $\rho_0$ .

It is natural to make the hypothesis of the continuity of  $\rho(r)$ : R is the radius for which the density  $\rho(r)$  of the concentration of dark substance is equal to  $\rho_0$  to obtain the radius R of the concentration of dark matter constituting the galaxy. We will call R the *dark radius* of the galaxy. So we have the equation:

$$\rho(R) = \rho_0 \tag{15}$$

The equation according to (7) and (8):

$$\frac{k_2}{4\pi R^2} = \rho_0 \tag{16}$$

$$\frac{2k_0T}{G} \times \frac{1}{4\pi R^2} = \rho_0 \tag{17}$$

So we obtain that the radius R of the concentration of dark substance constituting the galaxy is given approximately by the equation:

$$R = \left(\frac{2k_0T}{4\pi G\rho_0}\right)^{1/2} = K_4 T^{1/2} \qquad (18)$$

The constant K<sub>4</sub> being given by:

$$K_4 = (\frac{2k_0}{4\pi G\rho_0})^{1/2} \tag{19}$$

Then we consider that the sphere with a radius R of dark substance at the temperature T is in thermal interaction with the medium constituted of intergalactic dark substance at the temperature  $T_0$  surrounding this sphere. The simplest and most natural thermal transfer is the convective transfer. We stated this in the Postulate 2b):

Postulate 2b):

The thermal interaction between the spherical concentration of dark substance constituting the galaxy (with a density of dark substance in  $1/r^2$  and a homogeneous temperature T) and the surrounding intergalactic dark substance (at the temperature  $T_0$ ) can be modeled as a convective thermal transfer.

We know that if  $\varphi$  is the thermal flow of thermal energy on the borders of the spherical concentration of dark substance with a radius R,  $P_l$  being the total power lost by the spherical concentration of dark substance constituting the galaxy is given by the equation:

$$P_1 = 4\pi R^2 \phi \tag{20}$$

But we know that according to the definition a convective thermal transfer between a medium at a temperature T and a medium at a temperature  $T_0$  and according to the previous Postulate 2b) the flow  $\varphi$  between the 2 media is given by the expression, h being a constant depending only on  $\varphi_0$ :

$$\varphi = h(T-T_0) \tag{21}$$

The total power lost by the concentration of dark substance is:

$$P_1 = 4\pi R^2 h(T - T_0)$$
 (22)

We can consider that at the equilibrium, the total thermal power  $P_r$  received by the spherical concentration of dark substance constituting the galaxy is equal to the thermal power  $P_l$  lost by this spherical concentration. According to the equations (14) and (22), (M being the baryonic mass of the galaxy), we have:

$$K_3M=4\pi R^2 h(T-T_0)$$
 (23)

Using then the equation (18):

$$K_3M = 4\pi K_4^2 hT(T-T_0)$$
 (24)

Making the approximation  $T_0 << T$ :

$$M = 4\pi \frac{K_4^2}{K_2} h T^2$$
 (25)

Consequently we obtain the expression of T, defining the constant  $K_5$ :

$$T = \left(\frac{K_3}{4\pi K_4^2 h}\right)^{1/2} M^{1/2} = K_5 M^{1/2}$$
 (26)

And then according to the equation (10):

$$v^2 = 2k_0T = 2k_0K_5M^{1/2}$$
 (27)

So:

$$M = (\frac{1}{2k_0 K_5})^2 v^4 \tag{28}$$

So we finally obtain:

$$M = K_6 v^4$$
 (29)

The constant  $K_6$  being defined by:

$$K_6 = \left(\frac{1}{2k_0 K_5}\right)^2 = \frac{4\pi K_4^2 h}{4k_0^2 K_3} \qquad (30)$$

$$K_6 = \frac{4\pi h}{4k_0^2 K_3} \times \frac{2k_0}{4\pi G\rho_0}$$
 (31)

$$K_6 = \frac{m_0 h}{2k_0 G \rho_0 p_0} \tag{32}$$

We obtain the baryonic Tully-Fisher's law (12), with  $K_2=K_6$ . It is natural to assume that h depends on  $\rho_0$ . The simplest expression of h is  $h=C_1\rho_0$ ,  $C_1$  being a constant. With this relation,  $K_6$  is independent of  $\rho_0$ , and we can use the baryonic Tully-Fisher's law to define candles used to evaluate distances in the Universe.

## 2.4 Superposed sphere.

We consider a spherical concentration of dark substance with a density in  $1/r^2$  (that we defined in previous sections) moving in the space. We could expect that its velocity or its mass be modified because of its motion, of the Archimedes's force or of the absorption or of the loss of dark substance by the moving concentration of dark substance. This effect could be negligible, but we have a justification that it is nil much more interesting:

Indeed according to the new proposed model of dark matter, dark substance can own 2 possible behaviors: It can behave as a substance owning a mass or as absolute emptiness. For baryonic particles immerged inside dark substance, it always behaves as absolute emptiness and consequently the velocity of baryonic particles is never modified due to an Archimedes's force generated by the motion of baryonic particles through the dark substance. According to the new theory of dark matter, the intergalactic dark substance in which the spherical concentration of dark substance (with density in  $1/r^2$ ) is immerged also behaves as it was absolute emptiness concerning the displacement of this spherical concentration of dark substance are modified by its motion through the intergalactic dark substance. We will say that the spherical concentration of dark substance is a *superposed sphere* on the intergalactic dark substance surrounding it to interpret this phenomenon.

So we can define 2 kind of radius for a galaxy with a flat rotation curve: The 1<sup>st</sup> radius is the baryonic radius and the 2<sup>nd</sup> kind of radius is the dark radius, which is the radius of the superposed sphere containing the galaxy.

# 3.DISCUSSION

So the proposed model of dark matter is very attractive for the following reasons:

- (i)It explains the invisibility of dark matter and why particles of dark matter will never be observed, because dark substance constitutes what is called "emptiness". Dark substance is always both observed and not observed at the same time for any observer.
- (ii)It justifies the observations that dark matter does not interact through electromagnetic interaction for the same reason as (i).
- (iii)It justifies that collision between ordinary matter and dark substance has never been observed for the same reason as (i) and also because dark substance can behave as absolute emptiness.
- (iv)It permits to obtain the flat rotation curve of some galaxies very easily, using the very known law of ideal gas.
- (v)It permits to obtain very easily the baryonic Tully-Fisher's Law, using very simple thermal model.
- (vi)It is compatible with Newton's Laws for baryonic matter (Contrary to MOND).
- (vii)It is compatible with Special and General Relativity because it does not use any inertial frame.
- (viii) It is compatible with SCM.

Dark substance being a special substance, it does not own necessarily the same physical properties as ordinary baryonic matter. So we propose 2 fundamental properties for dark substance that are different from properties of ordinary matter:

The  $1^{st}$  property, called *double-behavior property* (of dark substance) has been exposed in the preceding section: Dark substance has the remarkable property of being able to behave sometimes as absolute emptiness and sometimes as ordinary matter with a mass. The fact that dark substance can also behave as absolute emptiness implies also the possibility that we must take  $T_0$ =0 in equation (21).

A  $2^{nd}$  fundamental property of dark substance, called *homogeneity property* (of dark substance) that we will admit is that sometimes it can tend to be homogeneous, its density not obeying to Newton's Law and sometimes its density obeys to Newton's Laws. This  $2^{nd}$  fundamental property is important because if we admit that at the scale of a star or of a black hole the tendency to homogeneity of dark substance predominates, then there is not concentration of dark substance around stars belonging to any galaxy. Consequently it exists 2 main kinds of galaxies: Galaxies belonging to a concentration of dark matter with a density of dark substance in  $1/r^2$ , as for instance the Milky Way and any galaxy with a flat rotational curve, and galaxies belonging to the intergalactic dark substance with a density of dark substance that is constant, as for instance Giant Elliptical Galaxies, in which few dark matter was detected.

The previous fundamental property permits also to interpret the observation of the curve of a galaxy G with a flat rotation curve close to  $O_G$  center of G. Close to  $O_G$  the density of dark substance cannot be in  $1/r^2$  because it would imply that it is infinite in  $O_G$  (which is not acceptable) and moreover because according to observation the rotation curve is not flat close to  $O_G$  (v( $O_G$ )=0, then v(r) increases with r. See Figure 2). This can be explained if we admit, using the previous homogeneity property of dark substance, that close to  $O_G$ , dark substance is homogeneous. This is true if we admit that the density of dark substance at a point P  $\rho$ (P) obeys to Newton's Law if we have the necessary condition  $\rho$ (P)< $\rho$ LIMH(T),  $\rho$ LIMH(T) being a given value that could (not necessarily) depend on the temperature T(P) of

the dark substance in P. Without this condition, the tendency to homogeneity predominates in P.

#### 4.BEYOND THE NEW MODEL OF DARK MATTER

The new model of dark matter can be generalized to larger scales than galaxies (galaxy clusters), to structure formation, and to interpret dark energy and the Cosmological parameters relative to the expansion of the Universe ( $\Lambda$ CDM model).

Indeed in the article [9] a model of dark matter inside galaxy clusters generalizing the preceding model is proposed. A first problem is that the proposed model is valid for an *ideal cluster*. An ideal cluster owns some properties (For instance it is spherical), and real clusters can only approximately be modeled as ideal clusters. A second problem is that the data permitting to verify the preceding model are not important in the SCM, so very few exist, moreover the few existing data possess a large margin of error. And those data are necessary to confirm or to invalidate this model. Nonetheless, the data relative to Coma Cluster and to Virgo Cluster, despite their important margin of error, are in good agreement with this model. Moreover, they permit to give an estimation of the dark radius of the Milky Way (≈500000 l.y), and of the mass of the Milky Way (≈1500 billions S.M) that are coherent with observations. But data relative to at least 15 galaxy clusters should be necessary to confirm or to invalidate this model. Those data should be obtained easily.

The previous model of dark matter in galaxy clusters is obtained using the previously called double-behavior property of dark substance. Indeed in this model we make the assumption using the preceding property that if a point P belongs to a concentration of baryonic matter (For instance a galaxy cluster or a concentration due to baryonic anisotropies in the early Universe) or to a concentration of dark substance (for instance a spherical concentration), then we must take in the Newton's equations the real density of dark substance, because then a kind of symmetry is broken at point P. But if it is not the case, then we must take a nil density at point P for dark substance in Newton's equations because there is a kind of symmetry at point P. For instance if the Universe was filled of baryonic matter completely homogeneous, according to the preceding property we should take  $\rho_{DS}(P)$ =0 at any point P in Newton's equations.

The previous property can be used in the models of structure formation relative for instance to the action of dark matter in the formation of galaxies.

We are now going to expose the interpretation of dark energy and of the Cosmological parameters ( $\Lambda$ CDM model) according to the proposed new model of dark matter. First we remark that dark energy cannot be the internal energy of dark substance considered as a gas because then it would evolve with the temperature of dark substance. But dark substance being a special substance, it can own a special energy, and we can make the simple assumption that dark energy is an energy of dark substance, analogous to the internal energy of an ideal gas, but that is directly proportional to the mass of the considered element of dark substance, and depending only of this mass. (We will have with evident notations  $E_S$ = $K_EM_{DS}$ ,  $K_E$  constant). With this simple assumption, the Cosmological parameter  $\Omega_{\Lambda}$  remains constant.

Concerning the Cosmological parameter  $\Omega_C$ , relative to the density of dark matter, we also remark that dark substance being a special substance, it does not necessarily contribute to the expansion of the Universe the same way as baryonic matter. So we can make the simple assumption that the density used in order to obtain the Cosmological parameter  $\Omega_C$  is not the real density of the dark substance but a density, called *effective density*, that is directly

proportional to the real density of dark substance. We will assume with evident notations that at any point P  $\rho_{EfDS}(P)=K_D\rho_{DS}(P)$ ,  $K_D$  constant. (According to the homogeneity property of dark substance, we will assume that the real density of dark substance (and therefore its effective density and the density of dark energy) is homogeneous in all the Universe, except inside spherical concentrations of dark substance constituting galaxies with a flat rotation curve).

With the 2 previous assumptions,  $\Omega_C$  and  $\Omega_\Lambda$  are constant, as is  $\Omega_B$ . Moreover, they a priori are independent (Because the preceding constants  $K_E$  and  $K_D$  are a priori independent), and therefore we can take for them the values predicted by the SCM (0,22 and 0,73).

### 5.A NEW GEOMETRIC MODEL OF UNIVERSE

The proposed model of dark matter permits also to define a new geometric model of Universe that is very close to the SCM: This geometric model is that Universe is a sphere in expansion, filled with dark substance and surrounded but something called *nothingness*. (We could assume that before the Big-Bang there was only nothingness). Then we keep all the elements of SCM (Including  $\Lambda$ CDM model), except the Cosmological Principle that is not true in all the Universe because in this model, Universe is isotropic only for an observer sufficiently far from its borders. At this condition, the Cosmological model will remain true. Of course we will admit that it is the case for an observer in our galaxy).

In the article [9], a new Cosmological model, different from SCM, but using the previous geometric model (spherical Universe in expansion surrounded by nothingness), is proposed. In this new Cosmological model, Universe is flat (in agreement with SCM), and 2 mathematical models of expansion are proposed: The 1<sup>st</sup> mathematical model uses the same mathematics as the SCM and the 2<sup>nd</sup> mathematical model is very simple (Constant velocities of expansion). Both mathematical models give predictions in good agreement with observation for z<12, but at larger z (For instance z corresponding to the apparition of CMB), observations (and especially observations of the anisotropies of the CMB), contradict the 2<sup>nd</sup> mathematical model and confirm the 1<sup>st</sup> mathematical model. But because according to SCM, the Universe is flat, we can easily generalize the simple properties of the 2<sup>nd</sup> mathematical model (that are exposed in details in the previously cited article) to the 1<sup>st</sup> mathematical model. This new Cosmological model is attractive because it is physically simpler than the SCM, because it gives the interpretation of the CMB rest frame, that is not interpreted by the SCM, and also because other topics.

## 6.CONCLUSION

In this article, we have modeled dark matter as a dark substance whose the physical properties, and in particular the fact that it can be modeled as an ideal gas, permitted to interpret 2 fundamental astronomical observations linked to dark matter. For instance, those physical properties permitted us to justify theoretically the flat rotation curve of galaxies and the baryonic Tully-Fisher's law. To obtain this, we interpreted galaxies with flat rotation curve as spherical concentrations of dark substance in gravitational equilibrium. We also obtained the density of dark substance close to the center  $O_G$  of a galaxy with a flat rotation curve. Our model of dark matter justified the invisibility of this dark matter.

We have studied according to our theory of dark matter the effects of the displacement of a concentration of dark substance on its mass and its velocity, and we have seen that those effects were nil. We saw that this theory permitted to define mathematically completely 2

kinds of radius for galaxies: The baryonic radius and the dark radius. We then exposed according to this theory the different models of distribution of dark matter in galaxies.

We have seen that the new model of dark matter was compatible with SCM.

Indeed we have seen that the new model of dark matter introduced in order to justify the flat rotation curve of galaxies and the Tully-Fisher's Law can be generalized in order to interpret dark matter at larger scales than galaxies (Galaxy cluster), dark matter in structure formation, dark energy and also Cosmological parameters relative to the expansion of the Universe (ACDM model).

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